

SIGNALS AND SYSTEMS

1. What is SIGNALS AND CLASSIFICATION OF SIGNALS?

Ans. A signal is a function representing a physical quantity or variable, and typically it contains information about the behavior or nature of the phenomenon. For instance, in a RC circuit the signal may represent the voltage across the capacitor or the current flowing in the resistor. Mathematically, a signal is represented as a function of an independent variable t . Usually t represents time. Thus, a signal is denoted by $x(t)$.

2. What are the Properties of the Convolution Integral?

Ans. The convolution integral has the following properties.

1. Commutative:

$$x(t) * h(t) = h(t) * x(t)$$

2. Associative:

$$(x * h_1) * h_2 = x * (h_1 * h_2)$$

3. Distributive:

$$x(t) * (h_1(t) + h_2(t)) = x(t) * h_1(t) + x(t) * h_2(t)$$

3. What are Causal and Stable Systems?

Ans. If the system is both causal and stable, then all the poles of $H(s)$ must lie in the left half of the s -plane; that is, they all have negative real parts because the ROC is of the form $\text{Re}(s) > a_{\max}$, and since the $j\omega$ axis is included in the ROC, we must have $a_{\max} < 0$.

4. Define Z-Transform?

Ans. The function $H(z)$ in Eq. (4.2) is referred to as the z -transform of $h[n]$. For a general discrete-time signal $x[n]$, the z -transform $X(z)$ is defined as

$$X(z) = \sum_{n=-\infty}^{\infty} x[n] z^{-n} \quad (4.3)$$

The variable z is generally complex-valued and is expressed in polar form as where r is the magnitude of z and θ is the angle of z . The z -transform defined in (4.3) is often called the bilateral (or *two-sided*) z -transform in contrast to the unilateral.

5. Define impulse response of a DT system.

Ans. The impulse response is the output produced by DT system when unit impulse is applied at the input. The impulse response is denoted by $h(n)$. The impulse response $h(n)$ is obtained by taking inverse Z transform from the transfer function $H(z)$

6. State Sampling theorem.?

Ans. A band limited signal of finite energy, which has no frequency components higher than the W hertz, is completely described by specifying the values of the signal at the instant of time separated by $1/2W$ seconds and

A band limited signal of finite energy, which has no frequency components higher than the W hertz, is completely recovered from the knowledge of its samples taken at the rate of $2W$ samples per second.

7. What are the Properties of ROC.?

Ans.

- i. The ROC of a finite duration sequence includes the entire z - plane, except $z=0$ and $|z|=\infty$.
- ii. ROC does not contain any poles.
- iii. ROC is the ring in the z -plane centered about origin.
- iv. ROC of causal sequence (right handed sequence) is of the form $|z| > r$.
- v. ROC of left handed sequence is of the form $|z| < r$.
- vi. ROC of two sided sequence is the concentric ring in the z plane

8. State convolution property of Z transform?

Ans. The convolution property states that if

$x_1[n]$
 $X_1(Z)$ and
 $x_2[n]$
 $X_2(Z)$ then
 $x_1[n] * x_2[n]$

$X_1(Z) X_2(Z)$

That is convolution of two sequences in time domain is equivalent to multiplication of their Z transforms